

LA-UR-14-27991

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Intended for: Geophysical Research Letters

Issued: 2014-10-14

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1 **Electron and ion heating by whistler turbulence:**
2 **Three-dimensional particle-in-cell simulations**

3
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5 10 October 2014

6 **Abstract**

7 Three-dimensional particle-in-cell simulations of decaying whistler turbulence are carried
8 out on a collisionless, homogeneous, magnetized, electron-ion plasma model. The
9 simulations use an initial ensemble of relatively long wavelength whistler modes with a
10 broad range of initial propagation directions with an initial electron beta $\beta_e = 0.05$. The
11 computations follow the temporal evolution of the fluctuations as they cascade into
12 broadband turbulent spectra at shorter wavelengths. Three simulations correspond to
13 successively larger simulation boxes and successively larger wavelengths of the initial
14 fluctuations. The computations confirm previous results showing electron heating is
15 preferentially parallel to the background magnetic field \mathbf{B}_0 , and ion heating is
16 preferentially perpendicular to \mathbf{B}_0 . The new results here are that larger simulation boxes
17 and longer initial whistler wavelengths yield weaker electron heating, stronger ion
18 heating, and weaker overall dissipation.

19
20 **Introduction**

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Solar wind protons, as they flow away from the Sun in a slowly decreasing magnetic field, should become strongly anisotropic in the sense of $T_{\perp} \ll T_{\parallel}$ due to conservation of their magnetic moments (Here \perp and \parallel denote directions relative to the background magnetic field \mathbf{B}_0). But proton velocity distributions near 1 AU are typically observed to be relatively isotropic, indicating that one or more plasma processes are acting to scatter such particles from parallel toward perpendicular velocities [Hellinger *et al.*, 2011; 2013]; an exhaustive list of possible such processes is presented in Section 2 of Cranmer [2014]. Two of the more popular of these processes are nonresonant ion scattering by low-frequency, long-wavelength magnetohydrodynamic (MHD) fluctuations including a nonlinear mechanism called “stochastic heating” (Chandran *et al.*, 2010; Xia *et al.*, 2013 and citations therein), and quasilinear ion cyclotron resonant scattering by Alfvén-cyclotron fluctuations somewhat below the proton cyclotron frequency and $k_{\parallel}c/\omega_p \leq 1$ (Hollweg and Isenberg, 2002; Gary and Saito, 2003; Cranmer, 2014, and citations therein) where ω_p denotes the proton plasma frequency. Recently Saito and Nariyuki [2014] used two-dimensional particle-in-cell (PIC) simulations to show that decaying whistler turbulence can transfer energy to ions preferentially in directions perpendicular to \mathbf{B}_0 , thereby arguing that whistler turbulence can also be a contributing mechanism to ion heating in the solar wind. This manuscript describes three-dimensional (3D) PIC simulations which extend the work of Saito and Nariyuki [2014] and in particular demonstrate that the perpendicular ion heating by whistler turbulence becomes stronger as successively longer wavelength fluctuations are considered.

Turbulence may be defined as an ensemble of enhanced, incoherent, broadband
 fluctuations. Such phenomena in magnetized, collisionless, ionized media may be
 empirically divided into long-wavelength plasma turbulence, with magnetic fluctuation
 spectra following a power-law wavenumber dependence $\sim k^{5/3}$ (the “inertial range”), and
 short-wavelength plasma turbulence, with much steeper fluctuation spectra $\sim k^{-\alpha}$ where α
 > 2 (the “kinetic range”). Solar wind observations of plasma turbulence spectra conclude
 that the spectral break between the two ranges scale approximately as $k\lambda_p \sim 1$, where λ_p is
 the proton inertial length [Bourouaine *et al.*, 2012], or as $k\rho_p \sim 1$, where ρ_p is the thermal
 proton gyroradius, or as a combination of these two scales and the fluctuation amplitude
 at those scales [Markovskii *et al.*, 2008]. The thermal proton beta β_p of the solar wind is
 typically of order unity, so it has been difficult to resolve the wavenumber scaling of this
 spectral break in that medium. However, there is general agreement that the spectral
 break marks the boundary between the long-wavelength regime in which fluid theories
 such as magnetohydrodynamics (MHD) provide an adequate description of the
 turbulence and the short-wavelength regime which requires a velocity-space (i.e.,
 “kinetic”) description of the turbulence.

Two competing hypotheses have been proposed to describe the character of short-
 wavelength turbulence in the solar wind. One scenario is that this turbulence consists of
 kinetic Alfvén waves which propagate in directions quasi-perpendicular to the
 background magnetic field \mathbf{B}_0 and at real frequencies $\omega_r < \Omega_p$ where the latter symbol
 represents the proton cyclotron frequency. Both solar wind observations [Leamon *et al.*,
 1998; Bale *et al.*, 2005; Sahraoui *et al.*, 2009, 2010; He *et al.*, 2012; Salem *et al.*, 2012;

67 *Chen et al.*, 2013, *Kiyani et al.*, 2013] and gyrokinetic simulations [*Howes et al.*, 2008a,
 68 2008b, 2011; *Matthaeus et al.*, 2008; *TenBarge et al.*, 2013] of turbulence have been
 69 interpreted as consisting of kinetic Alfvén waves. While it is likely that the turbulence
 70 measured immediately above the inertial range spectral break does consist of kinetic
 71 Alfvén waves, there is debate as to whether or not such modes can cascade fluctuation
 72 energy down to the very short wavelengths of electron inertial ($k\lambda_e \sim 1$) or thermal
 73 electron gyroradius ($k\rho_e \sim 1$) scales [*Podesta et al.*, 2010; *Smith et al.*, 2012; *Sahraoui et*
 74 *al.*, 2013]. A second hypothesis is that magnetosonic-whistler fluctuations between the
 75 proton cyclotron and electron cyclotron frequencies also contribute to such turbulence.
 76 Solar wind measurements provide evidence for magnetosonic-whistler and Bernstein
 77 mode contributions to short-wavelength turbulence [*Narita et al.*, 2011; *Perschke et al.*,
 78 2013, 2014]. Particle-in-cell simulations have been used to address the forward cascades
 79 of magnetosonic turbulence [*Svidzinski et al.*, 2009] and whistler turbulence [*Saito et al.*,
 80 2008, 2010; *Saito and Gary*, 2012; *Chang et al.*, 2011, 2013, 2014; *Gary et al.*, 2008,
 81 2012].

82
 83 Whistler PIC simulations show in particular that forward cascades give rise to
 84 turbulence with a preference for quasi-perpendicular propagation relative to \mathbf{B}_0 . This
 85 $k_{\perp} \gg k_{\parallel}$ wavevector anisotropy implies that whistler modes at $kc/\omega_e < 1$ should have
 86 substantial parallel electric field components, so that the Landau resonance is the primary
 87 means of wave dissipation on the magnetized electrons and the consequent heating
 88 should yield $T_{\parallel e} > T_{\perp e}$ as the body of PIC whistler turbulence simulations have
 89 demonstrated. The same wavenumber anisotropy further implies that the electrostatic

component of the fluctuating electric fields should provide the dominant contribution to δE [e.g., Fig. 6.8 of *Gary* (1993)], so that the primary heating on the relatively unmagnetized ions should yield $T_{\parallel i} < T_{\perp i}$, as has been argued by *Saito and Nariyuki* [2014] and as their simulations have demonstrated.

Whistler turbulence PIC simulations have, except for *Saito and Nariyuki* [2014], addressed only electron heating, but *Howes* [2010] used a cascade model to conclude that kinetic Alfvén turbulence should preferentially heat ions at $\beta_i > 2.5$, and heat electrons more strongly at smaller values of the ion beta [*TenBarge and Howes*, 2013]. This manuscript reports PIC simulations of decaying whistler turbulence with analyses of how the field fluctuation energy is dissipated on both the electrons and the ions. Consistent with the results of *Saito and Nariyuki* (2014), the ions are heated with $T_{\perp i} > T_{\parallel i}$, although more weakly than the electrons with $T_{\parallel e} \gg T_{\perp e}$. Here we quantitatively compare electron and ion heating for several different simulation box sizes, demonstrating that the relative ion heating increases as larger simulation systems admit longer wavelengths which allow the ion Landau resonance to become stronger.

Simulations

The simulations described here are carried out using the three-dimensional (3D) electromagnetic particle-in-cell code 3D-EMPIC which is a further development of the code described by *Wang et al.* [1995]. Here “three-dimensional” means that the simulations includes variations in three spatial dimensions, as well as calculating the full

3D velocity-space response of each ion and electron superparticle. With this code, superparticles are advanced using a standard relativistic particle algorithm, currents are computed using a rigorous charge conservation scheme [Villasenor and Buneman, 1992], and the self-consistent electromagnetic fields are solved using a local finite difference time domain solution to the full Maxwell's equations.

Our simulations model a collisionless, homogeneous, magnetized electron-ion plasma. The problem addressed is the same as that studied by *Chang et al.* [2011, 2013, 2014] and *Gary et al.* [2012]; an ensemble of relatively long-wavelength, approximately isotropic whistler fluctuations are imposed at $t=0$, and the simulations follow the subsequent temporal evolution of the fluctuating fields and the particles. The whistler modes undergo a forward cascade to a broadband turbulent spectrum at shorter wavelengths, while at the same time the plasma is heated. One important difference between the *Chang et al.* simulations and the computations described here is the initial conditions on the ions. The earlier simulations were concerned only with the interactions between the fluctuations and the electrons, so that the initial ion velocity distributions were taken to be Maxwellian. Here we wish to compare electron and ion heating, so that we have taken care to initialize both the electron and ion velocity distributions to reflect both species responses to the initial spectrum of whistler waves.

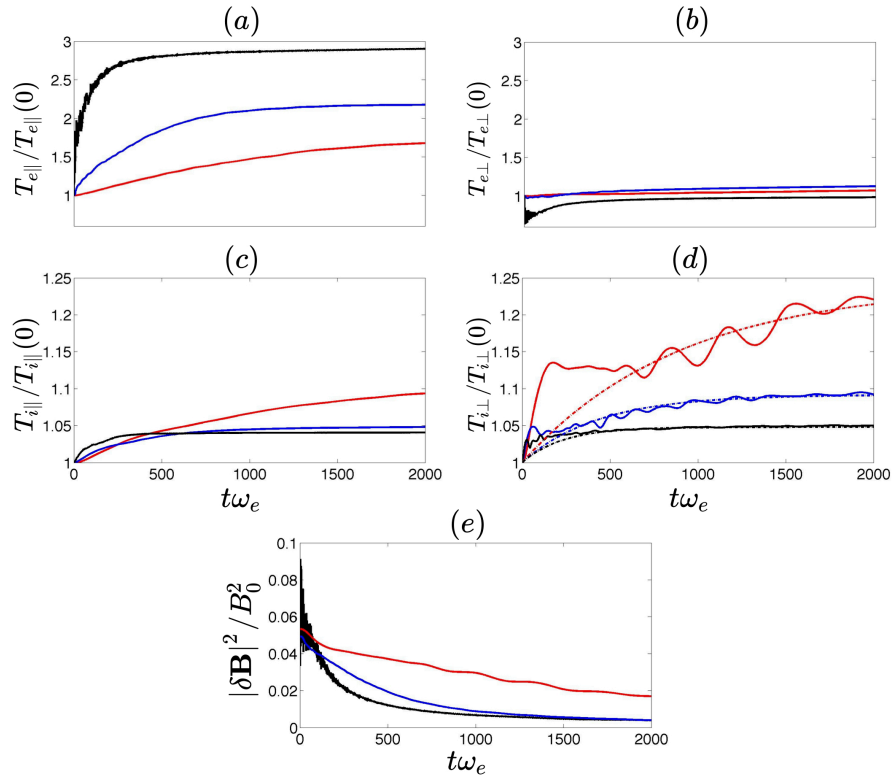
Our earlier PIC simulations of whistler turbulence evaluated the transfer of field fluctuation energy only to the electrons. Here, following *Saito and Nariyuki* [2014], we examine the ion heating as well. To facilitate the comparison of dissipation on both

species, we use $m_i/m_e = 400$; other physical initial conditions include isotropic Maxwellian velocity distributions for both species with $T_e = T_i$, $\beta_j \equiv 8\pi n_j k_B T_j / B_o^2$ where $j = e$ for electrons and $j = i$ for ions with $\beta_e = \beta_i = 0.05$. The electron thermal speed is denoted by $v_e = (k_B T_e / m_e)^{1/2}$ and at $t = 0$ $v_e^2 / c^2 = 0.01$. The initial dimensionless fluctuating magnetic field energy density is defined as $\epsilon_o \equiv \sum_k |\delta \mathbf{B}(\mathbf{k})|^2 / B_o^2$, and we choose $\epsilon_o = 0.10$.

The computational parameters are as follows: the grid spacing is $\Delta = 0.10 c / \omega_e$ where ω_e is the electron plasma frequency, the time step is $\delta t \omega_e = 0.05$, and the number of superparticles per cell is 64 with 32 electrons and 32 ions. Our simulations are carried out on a cube of size $L_x = L_y = L_z = L$. We have executed three computations at $L \omega_e / c = 25.6, 51.2$, and 102.4 , corresponding respectively to $256^3, 512^3$, and 1024^3 simulation cells and fundamental wavenumbers of, respectively, $k_{xo} c / \omega_e = 0.2454, 0.1227$, and 0.0614 . The initial spectra then correspond to arrays of 150 whistler modes that are relatively isotropic (The $k_\perp = 0$ whistler modes have well-defined dispersion properties, but there are no whistler fluctuations at $k_\parallel = 0$.), distributed as described in *Gary et al.* [2012].

Here our concern is the relative heating of electrons versus ions, and that comparison is shown in Figure 1. The first four panels of this figure confirm earlier simulation results that whistler turbulence preferentially heats electrons in directions parallel to \mathbf{B}_o [*Saito et al.*, 2008; *Gary et al.*, 2012; *Chang et al.*, 2013], and preferentially heats ions in directions perpendicular to the background magnetic field [*Saito and*

Nariyuki, 2014]. Comparison of panels (a) and (d) of Figure 1 shows a new result, that the longer wavelength whistler turbulence associated with larger simulation boxes provides less dissipative energy to the electrons but more such energy to the ions. Furthermore, Figure 1e shows that, for these three simulations, the total dissipation of the magnetic field fluctuations decreases as the simulation box size (and the overall wavelengths of the turbulence) increases. This is consistent with Fig. 7(b) of *Saito et al.* [2008] which shows linear theory damping of whistlers at quasi-perpendicular propagation decreasing as wavelengths increase. The linear theory damping is due to the Landau wave-particle resonance, and we infer that the same mechanism is heating the electrons and the ions in our simulations although nonlinear processes certainly contribute to the heating as the fluctuation amplitudes increase [e.g., *Chang et al.*, 2014].



171

172 **Figure 1.** Simulation histories of the (a) parallel electron, (b) perpendicular
173 electron, (c) parallel ion and (d) perpendicular ion temperatures as functions of time from
174 the runs with 256^3 cells (black lines), 512^3 cells (blue lines), and 1024^3 cells (red lines).
175 Panel (e) shows the simulation histories of the total magnetic field fluctuation energy for
176 the same three cases. The dashed lines represent fits to the equation $T_{\perp i}/T_{\perp i}(0) = 1 +$
177 $a[1-\exp(-bt)]$ with $a=0.048$ and $b=0.0043$ for the 256^3 run, $a=0.092$ and $b=0.0023$ for
178 the 512^3 run, and $a=0.240$ and $b=0.0011$ for the 1024^3 run.

179

180 Figure 2 illustrates the reduced electron parallel velocity distributions and ion
181 perpendicular velocity distributions at selected times for each of the three simulations.
182 The figures show that the transfer of fluctuation energy to both the electrons and ions is
183 indeed a heating process, because the late-time velocity distributions of both species for
184 the most part retain their thermal, Maxwellian-like character even as they gain energy.
185 The primary late-time departures from Maxwellian forms are on the electron parallel
186 velocity distributions in the presence of enhanced high-speed “tails” for the runs at 256^3
187 and 512^3 . This feature is a typical electron response to obliquely propagating whistlers at
188 $\beta_e \ll 1$, and is discussed in detail in *Chang et al.* [2013].

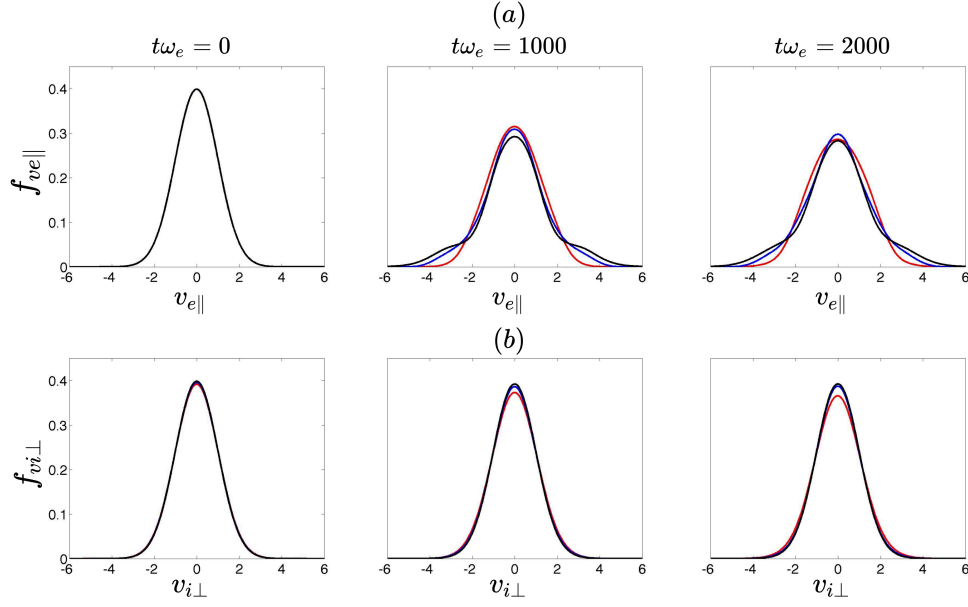


Figure 2. Reduced species velocity distributions from the three simulations at $\omega_e t = 0, 1000$, and 2000 as labeled for (upper row) electron parallel velocities and (lower row) ion perpendicular component velocities. Results are from the runs with 256^3 cells (black lines), 512^3 cells (blue lines), and 1024^3 cells (red lines).

Conclusions

We have used fully three-dimensional, fully kinetic particle-in-cell simulations to examine how decaying whistler turbulence in a low- β collisionless plasma dissipates energy on both electrons and protons. Our computations confirm previous results showing electron heating is preferentially parallel to the background magnetic field \mathbf{B}_0 , and ion heating is preferentially perpendicular to \mathbf{B}_0 .

The new results here are that larger simulation boxes and longer initial whistler wavelengths yield weaker electron heating, stronger ion heating, and weaker overall dissipation.

The interpretation of anisotropic electron and ion heating by whistler turbulence in the weak fluctuation limit is direct; the $k_{\perp} > k_{\parallel}$ wavevector anisotropy which usually results from the forward whistler cascade implies the Landau resonance dominates the wave-particle interactions at $kc/\omega_e < 1$ and yields preferential parallel heating on the electrons and perpendicular heating on the ions. The relative heating of the two plasma species as a function of the simulation box size requires a more involved interpretation, as follows. In the computations described above, a larger simulation box corresponds to larger values of the initial whistler wavelengths, so that the initial k_{\parallel} and k_{\perp} are both smaller. In the limits of $kc/\omega_i \gg 1$ and $kc/\omega_e \ll 1$, linear dispersion theory predicts that the whistler frequency is $\omega_r/\Omega_e \approx k_{\parallel} c^2/\omega_e^2$. Heating of the ions, which are essentially unmagnetized in response to the relatively high frequency whistler fluctuations, is by means of the Landau resonance at $v_{\perp} = \omega_r/k_{\perp} \approx (k_{\parallel} c/\omega_e) c\Omega_e/\omega_e$, so a larger simulation box and longer wavelengths correspond to a smaller resonant ion velocity. This implies that the resonant modes move from the tail of the perpendicular velocity distribution toward the thermal part of the distribution, resonating with a larger number of ions and therefore leading to stronger ion heating. Howes [2010] has proposed a scenario for plasma heating by kinetic Alfvén wave turbulence in which the maximum dissipation on the ions is at wavelengths of the order of the thermal ion gyroradius; the turbulent energy which remains is then carried by the forward cascade down to electron dissipation at thermal

electron gyroradii. Applying this scenario to magnetosonic-whistler turbulence, the assumed source of the long-wavelength initial fluctuations in our simulations, the increasing ion heating at larger simulation box sizes leaves successively less energy at electron fluctuation scales, implying, as our simulations demonstrate, less electron heating.

Further simulations are necessary to gain a more complete understanding of how short-wavelength turbulence dissipates its energy in collisionless plasmas. It would be useful to examine the relative heating of electrons and ions by whistler turbulence as functions of the dimensionless parameters β_e , ε_o and T_e/T_i , particularly toward values appropriate for the solar wind near 1 AU, that is, $\beta_e \approx 1$ and $\varepsilon_o \ll 1$. Each of these parametric studies can be addressed now using available supercomputer resources. It would be interesting to compare the ion/electron heating ratio as a function of the initial whistler fluctuation energy density against the large-scale turbulence PIC simulation results of *Wu et al.* [2013] which show an increase in this ratio with increasing initial fluctuation energy.

However, perhaps the most important parametric study of this type concerns variations in the characteristic wavelengths of the turbulence. As longer wavelength fluctuations correspond to weaker electron and stronger ion heating and turbulent spectra usually increase in amplitude with increasing wavelength, it is important to push 3D PIC simulations to the regime of $kc/\omega_e < 0.05$. Unfortunately, this requires the calculations to be carried out in successively larger simulation boxes, requiring computational resources that are not available to most researchers pursuing this subject (However, see *Karimabadi et al.*, 2013). As computing capacity continues to increase, our ability to more

completely address the important issue of short-wavelength turbulent dissipation will similarly increase.

Acknowledgments. The research by R. Scott Hughes, S. Peter Gary, and Joseph Wang was supported largely by the National Science Foundation (NSF) grant AGS-1202603 under the NSF/DOE Partnership in Basic Plasma Science and Engineering. Computational resources supporting this work were provided by the NASA High-End Computing (HEC) Program through the NASA Advanced Supercomputing (NAS) Division at Ames Research Center, as well as by the Yellowstone supercomputer sponsored by the NSF at the Computational and Information Systems Laboratory of the National Center for Atmospheric Research. The computer-generated data used to produce the results described here are archived at the University of Southern California and are available from Dr. Joseph Wang.

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